III. Observations concerning the Height of the Barometer, at different Elevations above the Surface of the Earth, in a Letter to the Publisher from the Learned Dr. Nettleton.

SIR,

BEING curious to learn by Observation, how far the Mercury will descend in the Tube at any given Elevation, for which there is sufficient Opportunity hereabouts, I proposed to take the Altitude of some of our highest Hills; but, when we attempted it, we found our Observations so disturbed by Refractions, that we cou'd come to no Certainty. Having measur'd one Hill of a confiderable Height, in a clear Day, and obferved the Mercury at the Bottom and at the Top, we found, according to that Estimation, that about 90 Feet, or upwards, were required to make the Mercury fall one Tenth of an Inch; but coming afterwards to repeat the Experiment on a cloudy Day, when the Air was fornewhat gross and hazy, we found the small Angles so much augmented by Refraction, as to make the Hill much higher than before, tho' they were taken carefully with very good Instruments, both at that Time and be-I afterwards frequently observed at home, by pointing the Quadrant to the Tops of some of our neighbouring Mountains, that they wou'd appear higher in the Morning before Sun-rife, and also late in the Evening, than at Noon, in a clear Day, by feveral Minutes: Particularly, one Morning in December last, when the Vapours lay condens'd in the Vallies, and the Air above was very pure, the Top of a Mountain, at some Distance from from hence, appear'd more elevated, by above 30 Minutes, than it had done in the Beginning of September about Noon, on a very clear Day. From whence it appears, that the Refraction is at some times greater than at others; but probably 'tis always very considerable, and, as there is no certain Rule to make Allowance for it, it seems likely, that all Observations made on very high Hills, especially when view'd at a Distance, and under small Angles, as they commonly are, are uncertain, and scarce to be depended on, generally erring in making the Heights greater than they really are.

I then proceeded to observe, as near as I was able, the section of the Mercury in some smaller perpendicular discretions, which we cou'd measure with a Line, and also on the Tops of some Hills of a moderate Height, whose Altitude we cou'd observe most commodiously, and, by taking the Angles large, avoid the Danger of any considerable Refraction.

At the Bottom of the Tower of *Halifax* Church, the Mercury flood at 29 *Inch.* 78 *Dec.* At the Top it subsided to 29. 66. The Height of the Place, where the Observation was made, was found to be 102 Feet.

At the Bottom of a Coal-Mine, near this Place, the Mercury stood at 29. 48. At the Top, it fell to 29. 32. The Depth of the Mine, being measured, was found to be 140 Feet.

At the Bottom of another Mine, the Mercury was obferved to stand at 29.50. At the Top, it fell to 29.23. The Depth of this Mine was 236 Feet.

At the Foot of a small Hill, whose Height we cou'd measure very exactly, the Mercury stood at 29.81. At the Top it fell to 29.45. The Height of the Hill was 312 Feet.

At the Bottom of Halifax Hill, commonly call'd the Bank, the Mercury was observed to stand at 30.00.

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At the Top, it fell to 29. 41. The Height of this Hill was found to be 507 Feet.

Our Mathematicians do demonstrate, that the Density of the Air decreases in a Geometrical Progression, as the Elevation encreases in an Arithmetical one, and consequently, that the Logarithms of the Densities are as the Elevations reciprocally. But the Weight of the Air being as its Density, and the Height of the Mercury in the Barometer being always proportional to the Air's Weight, it follows, that the Logarithms of the Heights of the Mercury are, reciprocally, as the Elevations: Whence having found by Observation, what Elevation is required to make the Mercury stand at any Height, it will be easy to determine, how much is requisite to reduce it to any other Height proposed. If

quisite to reduce it to any other Height propos'd. If we make 30 Inches the Standard Height of the Mercury, equal to Unity, and suppose an Elevation of 85 Feet be requir'd to make it fall one Tenth of an Inch from that Height, as by these Observations it is very nearly;

then as the Logarithm of $\frac{30.0}{29.9}$ is to 85, so is the Log.

29.5 to the Number of Feet required to make it fall

Half an Inch, and so of the rest. When the Mercury stands above 30 Inches, the Numbers will be negative, and shew the Spaces descending; by which Method I

computed the following Tables.

The latter, which contains the Differences of the Numbers in the former, was of very great Use to me, when, in these Experiments, the Mercury stood at any other Height in the Tube, besides 30 Inches, and fell any Number of Tenths, or Parts of a Tenth, by adding the Numbers answering thereto, or proportionable Parts of them, to find the Elevation requir'd in the Table, to make the Mercury fall so much, and thereby readily

to compare the Heights found by Observation therewith. And though some small Errors, in the Observations, do make them vary a little from each other, yet in the main, they agree as near as possible with the Numbers of the Table; as did also several other Experiments too long to mention, which makes me believe those Numbers are not far from the Truth; but of that you will be best able to judge, by comparing these Experiments with others of the same Kind.

That the Air is colder, as well as more light and rare, in Places that are fituated high, than it is in the Vallies and low Grounds, is generally known; and in order to learn, how much it might be so, I got a Friend of mine, who lives higher than we do here, to observe the portable Barometer and Thermometer, at his House, for some Days, being plac'd as near as possible in the same Circumstances with mine; and we found his Barometer stood at a Medium for 20 Days, 3 Tenths lower than mine, and the Thermometer 3. deg. 2. lower; allowing for the Difference of the Instruments, which had been observed before.

At another Place the Barometer, at a Medium for 14 Days, stood lower by 4.46. and the Thermometer was lower by 4. deg. 4. At another Place, which was very high upon the Moors, the Barometer, at a Medium for ten Days, stood lower by 0.65. and the Thermometer fell 72.

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A Table shewing the Number of Feet ascending, requir'd to make the Mercury sall to any given Height in the Tube, from 30 to 26 Inches. As also the Number of Feet descending, requir'd to make the Mercury rise, from 30 to 31 Inches.

A Table shewing the Number of Feet requir'd to make the Mercury fall one Tenth of an Inch from any given Height in the Tube, from 31 to 26 Inches.

In. Dec.	Feet Dec.	In. Dec.	Feet D	ec.		In. De	c. I	Peet	Dec.	In. Dec.	Feet 1	Dec.
30 30 30 30 30 30 30 30 30 30	169 18 84 7: 90 95 170 2 255 8 341 7 427 8 668 1 775 4 863 0 951 0 1127 8 1127 8 1127 8 11305 8 11395 3 1485 1 1575 2	27 7 6 5 4 3 2 2 7 6 5 4 3 2 2 6 2 6 6 5 4 4 8 1 5 0 6 3 2 3 6 0 0 0 6 3 2 3 6 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1938 2030 2122 2215 2307 2401 2494 2588 2682 2776 2871 2966 3062 3158 3254 3351	55 97 72 80 21 95 02 44 20 33 80 62 79 32 21 46 07 05 41 14		31 30 30 30 30 30 30 30 30 30 30	98 76 5 4 32 10 98 76 5 4 32 10 98 76 5 4 32	333334445555666677777888889999	79 06 33 61 89 16 44 72 09 58 66 45 74 03 33	27 6 27 27 27 27 27 27 27 26 26 26 26 26 26 26 26 26 26 26 26 26	92 92 93 93 94 94 95 95 96 97 97	42 75 08 41 74 07 41 76 12 47 82 17 53 89 36 73 10